

SubsetMex

Problem Name	Subset Mex
Input file	standard input
Output file	standard output
Time limit	1 second
Memory limit	256 megabytes

A *multiset* is a collection of elements similar to a set, where elements can repeat multiple times. For example, the following is a multiset:

$\{0, 0, 1, 2, 2, 5, 5, 5, 8\}$

Given a multiset S defined on non-negative integers, and a target non-negative integer value n such that n does not belong to S , your goal is to insert n into S by using the following 3-step operation, repeatedly:

1. Choose a (possibly empty) subset T of S . Here, T is a set of distinct numbers that appear in S .
2. Erase elements of T from S . (Remove only one copy of each element.)
3. Insert **mex**(T) into S , where **mex**(T) is the smallest non-negative integer that does not belong to T . The name **mex** stands for “minimum excluded” value.

Your goal is to find the minimum number of operations to perform so that n becomes part of S .

Since the size of S may be large, it will be given in the form of a list (f_0, \dots, f_{n-1}) of size n , where f_i represents the number of times that the number i appears in S . (Recall that n is the integer we are trying to insert into S .)

Input

The first line contains a single integer t ($1 \leq t \leq 200$) — the number of test cases. Each two of the following lines describe a test case:

- The first line of each test case contains a single integer n ($1 \leq n \leq 50$), representing the integer to be inserted into S .

- The second line of each test case contains n integers f_0, f_1, \dots, f_{n-1} ($0 \leq f_i \leq 10^{16}$), representing the multiset S as mentioned above.

Output

For each test case, print a single line containing the minimum number of operations needed to satisfy the condition.

Scoring

Subtask #1 (5 points): $n \leq 2$

Subtask #2 (17 points): $n \leq 20$

Subtask #3 (7 points): $f_i = 0$

Subtask #4 (9 points): $f_i \leq 1$

Subtask #5 (20 points): $f_i \leq 2000$

Subtask #6 (9 points): $f_0 \leq 10^{16}$ and $f_j = 0$ (for all $j \neq 0$)

Subtask #7 (10 points): There exists a value i for which $f_i \leq 10^{16}$ and $f_j = 0$ (for all $j \neq i$)

Subtask #8 (23 points): No additional constraints

Examples

standard input	standard output
2	4
4	10
0 3 0 3	
5	
4 1 0 2 0	

Note

In the first example, initially, $S = \{1, 1, 1, 3, 3, 3\}$ and our goal is to have 4 in S . We can do the following:

1. choose $T = \{\}$ then S becomes $\{0, 1, 1, 1, 3, 3, 3\}$
2. choose $T = \{0, 1, 3\}$ then S becomes $\{1, 1, 2, 3, 3\}$
3. choose $T = \{1\}$ then S becomes $\{0, 1, 2, 3, 3\}$
4. choose $T = \{0, 1, 2, 3\}$ then S becomes $\{3, 4\}$